## NUMERICAL PROBLEMS

Problem 13.1 At what distance from a long straight wire carrying a current of 10 A is the magnetic field is equal to the earth's magnetic field of 5 x 10<sup>-5</sup> T?

Solution

$$i = 10 A$$
  $B = 5 \times 10^{-5} T$ 

Using Ampere's circuital law  $B = \frac{\mu o i}{2\pi r}$ 

$$B = \frac{\mu \sigma T}{2\pi r}$$

$$r = \frac{\mu \sigma T}{2\pi B} = \frac{(4\pi \times 10^{-7})(10)}{2\pi (5 \times 10^{-5})} = 0.04m$$

Problem 13.2 A long solenoid has 1000 turns uniformly distributed over a length of 0.5m produces a magnetic field of 2.5x10-3T at the center. Find the current in the

solenoid?

Solution N = 1000

For a solenoid B = μ<sub>o</sub> n i

$$i = \frac{B}{\mu o n} = \frac{B \ell}{\mu o N} = \frac{(2.5 \times 10^{-3}) (0.5)}{4\pi \times 10^{-7} (1000)} = 1 A$$

Problem 13.3 A proton moving at right angle to magnetic field of 0.1T experience a force of 2x10<sup>-12</sup> N. what is the speed of the proton?

Solution

$$\theta = 90^{\circ}$$

$$B = 0.1 T$$

$$F = 2 \times 10^{-12} N$$
  $V = ?$   $q = e (proton)$ 

Force on a charge entering in a magnetic field is

$$F = q v B Sin\theta$$

$$V = \frac{F}{q B \sin \theta} = \frac{2 \times 10^{-12}}{(1.6 \times 10^{-19})(0.1)(\sin 90)}$$

$$v = 1.25 \times 10^{8} \text{ m/s}$$

Problem 13.4 An 8 MeV proton enters perpendicularly into a uniform magnetic field Problem 13.4 And wer proton entering the proton (b) what will be the radius of the path of

Solution

$$\theta = 90^{\circ}$$
 B = 2.5 T

Given that kinetic energy

$$K.E = \frac{1}{2} \text{ m v}^2$$

$$v = \sqrt{\frac{2 (K,E)}{m}} = \sqrt{\frac{2 (8 \times 10^{6}) (1.6 \times 10^{-19})}{1.67 \times 10^{-27}}} = 3.9 \times 10^{7} \text{ m/s}$$

Put value of "v" in equation (1) =

$$F = q v B Sin\theta = (1.6 \times 10^{-19}) (3.9 \times 10^{7}) (2.5) Sin90^{0}$$
  
 $F = 1.6 \times 10^{-11} N$ 

(b) The force F that the magnetic field exerts on proton provides necessary

centripetal force given by

$$F = \frac{m v^2}{r}$$

$$r = \frac{m v^2}{F} = \frac{(1.67 \times 10^{-27}) (3.9 \times 10^{7})^2}{(1.6 \times 10^{-11})} = 0.16 \text{ m}$$

#### Problem 13.5 A wire carrying current 10 mA experiences a force of 2 N in a uniform field. What is the force on it when current rises to 30 mA?

#### Solution

i 1 = 10 mA

$$F_1 = 2 N$$

$$F_1 = 2 N$$
  $i_2 = 30 m A$   $F_2 = ?$ 

$$F_2 = ?$$

F=i&B

For first conductor

$$F_1 = i_1 \ell B$$

=

$$\&B = \frac{F_1}{i_1} = \frac{2}{10 \times 10^{-3}} = 200 \text{ NA}^{-1}$$

Now for second conductor

Putting value of "& B" in above equation we get

$$F_2 = (30 \times 10^{-3})(200) = 6 N$$

#### Problem 13.6 What is the time period of an electron projected into a uniform magnetic field of 10 mT and moves in a circle of radius 6 cm?

$$B = 10 \times 10^{-3} T$$

$$q v B = \frac{m \cdot v^2}{r}$$
 ..... (1)  
 $v = r w = r \left(\frac{2\pi}{r}\right)$  ..... (2)

also

$$v = r w = r \left( \frac{2\pi}{T} \right)$$
 ----- (2)

putting eq (2) in eq (1) and re-arranging them we get

$$T = \frac{2 \pi m}{q B} = \frac{2 (3.14) (9.11 \times 10^{-31})}{(1.6 \times 10^{-19}) (10 \times 10^{-3})}$$

$$T = 3.6 \times 10^{-9} \text{ sec} = 3.6 \text{ n.sec}$$

#### Problem 13.7 A 0.2 m wire is bent into a circular shape and is placed in uniform magnetic field of 2T, if the current in the wire is 20 mA then find the maximum torque acting on loop?

Solution

€ = 0.2 m

$$B = 2T$$

$$i = 20 \text{ m A}$$
  $\tau_{\text{max}} = ?$ 

N = 1 and for maximum torque Cos  $\theta = 1$ 

$$\tau_{max} = B i A$$

Area for a wire is 
$$A = \pi r^2$$

$$\tau_{max} = B i \pi r^2$$
 .....(1)

When wire is bent into circle then its length is equal to circumference

$$\ell = 2 \pi r$$

$$r = \frac{\ell}{2 \pi} = \frac{0.0}{2 \cdot (3.0)}$$

 $r = \frac{\ell}{2\pi} = \frac{0.2}{2(3.14)} = 0.0318 \text{ m}$ 

Now putting this value of r in eq (1) above we get

 $\tau_{max} = 2 (20 \times 10^{-3}) (3.14) (0.0318)^2 = 1.27 \times 10^{-4} \text{ N m}$ 

#### Problem 13.8 Full scale deflection for galvanometer is 10 mA. Its resistance is 100 $\Omega$ . How it be converted into ammeter of range 100 A? Solution

ig = 10mA = 0.01A

 $R_g = 100 \Omega$   $R_s = ?$  for i = 100 A

In order to convert a galvanometer into an ammeter, we need a shunt resistor  $\mathbf{r}_{s}$  in parallel with galvanometer given by

$$R_{s} = \frac{i_{g} R_{g}}{(i - ig)} = \frac{(10 \times 10^{-3}) \ 100}{(100 - 0.01)}$$

$$R_{s} = 0.01 \Omega$$

# Problem 13.9 How 5mA, $100\Omega$ galvanometer converted to 20V voltmeter?

i = 5 m A

 $R_g = 100 \Omega$ 

 $R_h = ?$  for V = 20 Volts

#### Solution

In order to convert galvanometer into a voltmeter of 20 V range we connect a high resistance  $r_h$  in series with galvanometer and is given by

$$R_h = \frac{V}{i} - R_g = \frac{20}{0.005} - 100 = 3900 \Omega$$

### Problem 13.10 Two parallel wires 10 cm apart carry current in opposite direction of 8 A. what is the magnetic field halfway between them?

Solution

d = 10 cm

i = 8 A

B = ? at mid point

At mid-point

r = d/2 = 5 cm

Now B can be determined by Ampere's circuital law  $B = \frac{\mu_0 i}{2 \pi r} + \frac{\mu_0 i}{2 \pi r} = \frac{\mu_0 i}{\pi r} = \frac{(4 \pi x 10^{-7})(8)}{\pi (5 x 10^{-2})}$ 

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