

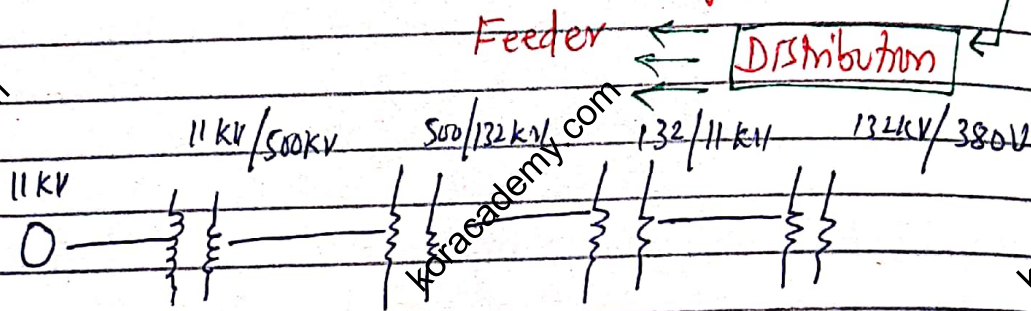
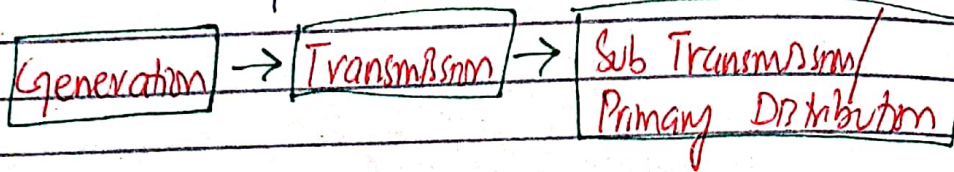
# POWER SYSTEM ANALYSIS.

17/11/20

William D Stevenson (3<sup>rd</sup> edition)

## Power System.

A network of electrical components that generates/transmits and supply/distribute electrical power to the load centres.



380 V Line to line voltage.

220 V Line to phase voltage.

## Transmission System.

Carries power from the generating end to the load centre.

Transmission lines are often known as connecting links b/w generator and load.

## Distribution system

It feeds power from the distribution grid station to the ~~feeders~~ load centres through feeders.

Transmission at 33kV, 66, 132, 220, 500, 1000, 1500kV

Breakdown of air = 30kV/cm

Why not use higher voltage?

- Insulation cost
- All equipment is for 220.
- Higher chances of accidents.


Generating stations are always balanced;


- Equal number of turns.
- Same material of all coils.
- Same resistance

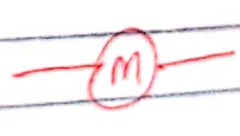
A three phase balanced system can always be replaced by a single phase system for analysis.



If we replace actual things by symbols  $\rightarrow$  single line diagram.

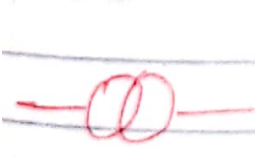
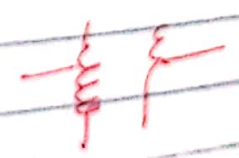
### Symbols

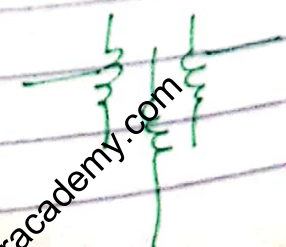
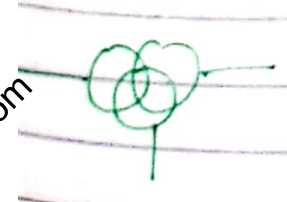
 rotating machine.

 generator

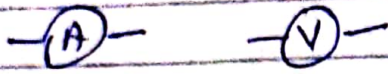
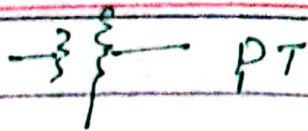
 motor etc

Current breaker  , 

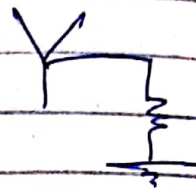
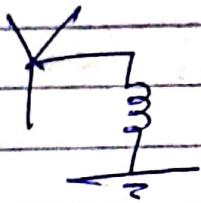
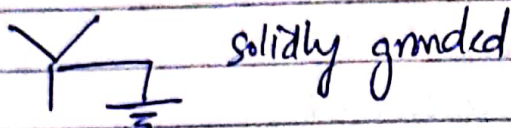


CT



Static load

Transmission Line

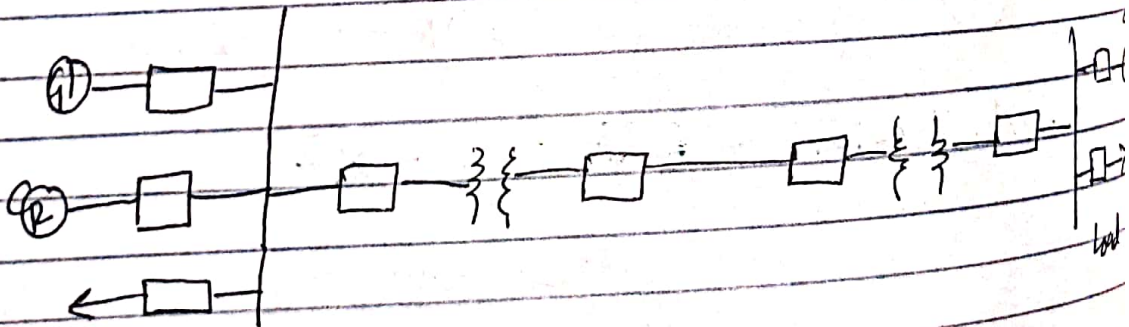


### Ground Fault Neutralizer / Peterson coil

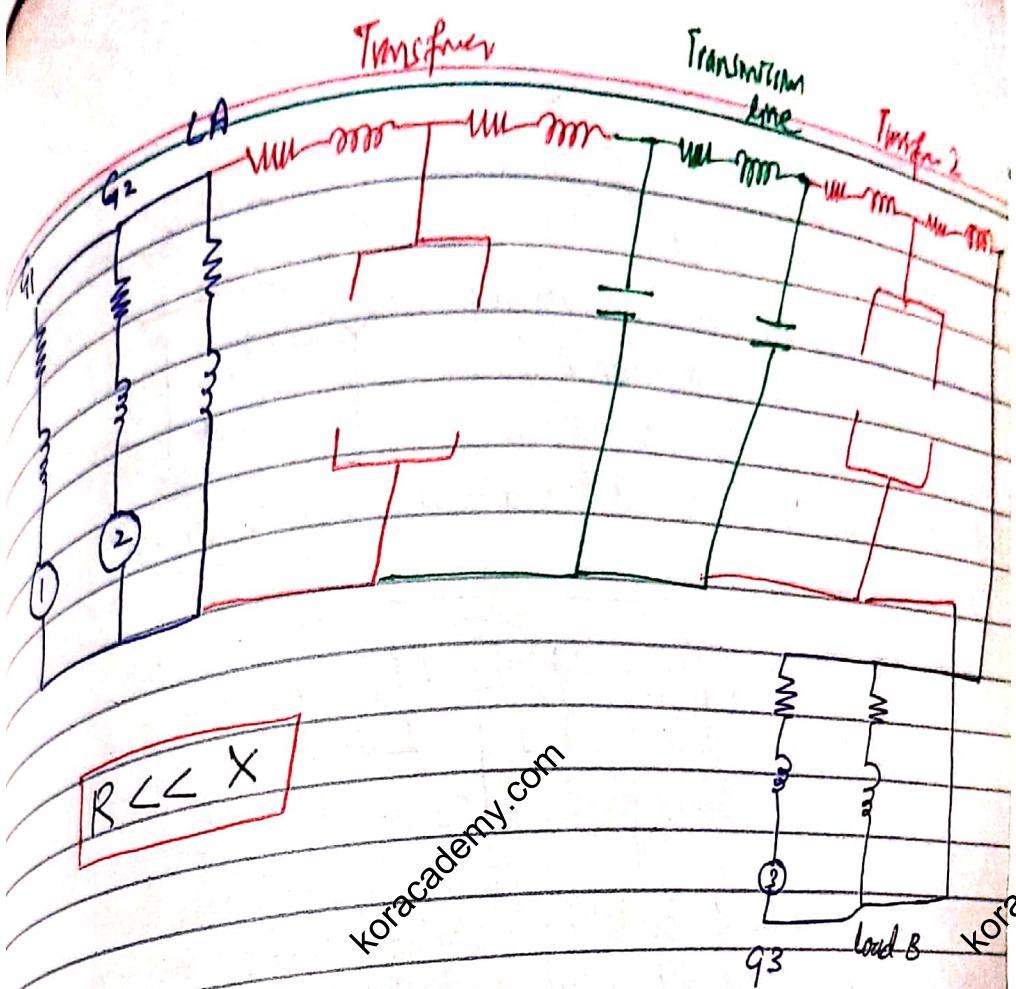
3  $\phi$  system is used b/c;

- It is economical
- Reduces conductor size.
- Reduces power losses.

**\*\*** Converting single line diagram into reactance diagram

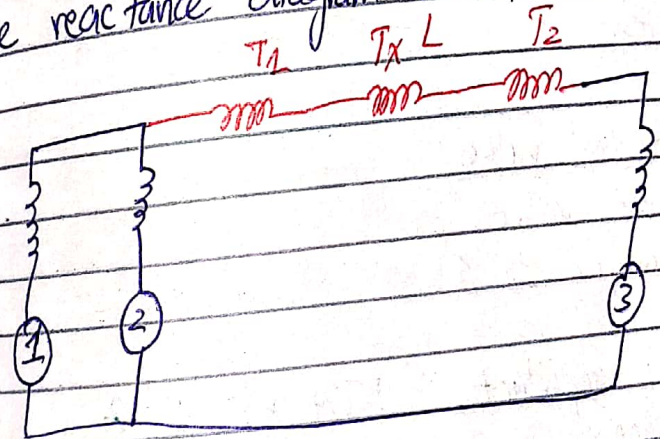


Load A



$$R \ll X$$

The reactance diagram is as:



Lecture 2

24/11/20

3 types of reactances;

- $X \rightarrow$  synchronous reactance.
- $X' \rightarrow$  transient reactance.
- $X'' \rightarrow$  subtransient reactance.

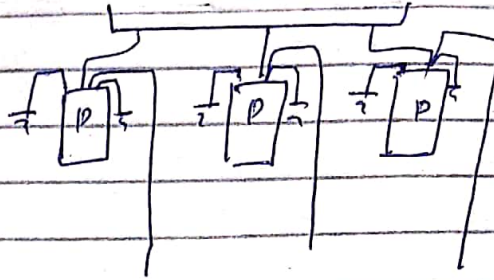
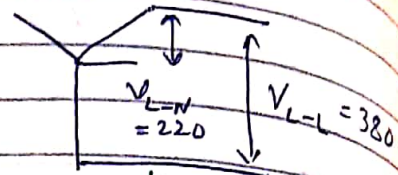
- All the data is 3 phase until mentioned.

- Voltages are always line to line

- Impedance provided is always a single phase impedance.

- Current is always for one line.

- Data provided for 3  $\phi$  bank is single phase data.



- Fault, Load, and stability study cannot be done with single line diagram.

### Per Unit System

$$Pu = \frac{\text{Actual value}}{\text{Base value}}$$

values are nearer to 1.

4 quantities are very important; KVA, KV, I, Z  
Select base quantity for 2 of them and derive for other two.

Normally select base, KVA and KV and derive for I and Z.

let KVA  $\rightarrow$  single phase KVA, Z  $\rightarrow$  per unit imp  
KV  $\rightarrow$  L-N voltage, I  $\rightarrow$  line current

$$(KVA)_b, (KV)_b$$

$$I = \frac{P}{V} = \frac{(KVA)_b}{(KV)_b} \quad \text{--- (1)}$$

$$Z_{base} = \frac{V_{base}}{I_{base}} = \frac{(KV)_b \times 1000}{(KV)_b \times 1000} \quad (2)$$

$$Z_{base} = \frac{(KV)_b^2 \times 1000}{(KVA)_b}$$

Base KVA = ~~18000~~ 3000

Actual = 18000 KVA, 120 KV  
108 KV

$$pu = \frac{18000}{3000} = pu \ 0.6$$

Similarly for single phase

$$pu = \frac{18000/3}{3000/3} = 0.6 pu$$

Similarly  $pu = \frac{108}{120} = 0.9 pu$

and  $pu = \frac{108/3}{120/3} = 0.9 pu$

Let  $(KVA)_b \rightarrow 3 \phi \ KVA$   $(KV)_b = L-L \ voltage$

$$I_b = \frac{(KVA)_b / 3}{(KV)_b / \sqrt{3}} = \frac{(KVA)_b \times \sqrt{3}}{(KV)_b \times 3}$$

$$I_{base} = \frac{(KVA)_b}{\sqrt{3}(KV)_b} \quad (3)$$

$$(I = \frac{P \ cos \ \theta}{\sqrt{3}V})$$

$$Z_{base} = \frac{\left(\frac{(KV)_b}{\sqrt{3}}\right)^2 \times 1000}{(KVA)_b / 3} = \frac{(KV_b)^2 \times 1000}{(KVA)_b}$$

$$= \frac{(KV_b)^2}{(MVA)_b}$$

Now.

$$Z_{pu} = \frac{Z_{actual}}{Z_{base}} = \frac{Z_{act}}{\frac{(KV_b)^2 \times 1000}{(KVA)_c}}$$

$$= \frac{Z_{act} \times (KVA)_b}{(KV_b)^2 \times 1000} = \frac{Z_{act} \times (MVA)_b}{(KV_b)^2}$$

$$Z_{pu} = K \frac{(MVA)_b}{(KV_b)^2}$$

$$Z_{pu} \text{ (new base)} = Z_{pu} \text{ (old base)} \times \frac{(KVA)_b \text{ (new)}}{(KVA)_b \text{ (old)}} \times \frac{(KV_b \text{ old})^2}{(KV_b \text{ new})^2}$$

- Such a base quantity is selected where per unit quantities become equal or closer to 1.

- KVA base, once selected, does not change for the entire circuit.

- KV base changes when you encounter a transformer.

It changes in accordance with transformation ratio.

- The specified per unit values are always specified on rating of the system.

The power of motor is mechanical power.

For induction motor;  $hp = KVA$   
 For synchronous machine at unity pf;  $KVA = 0.95 hp$   
 at 0.8 pf;  $KVA = 1.10 hp$

Let  $Z_{HT}$  - HT side impedance  
 $KV_L \rightarrow$  rated LV voltage  
 $Z_{LT}$  - LT side impedance  
 $KV_H \rightarrow$  rated HV voltage  
 $KVA \rightarrow$  KVA of transformer.

$$Z_{LT} = Z_{HT} \left( \frac{KV_{LT}}{KV_{HT}} \right)^2$$

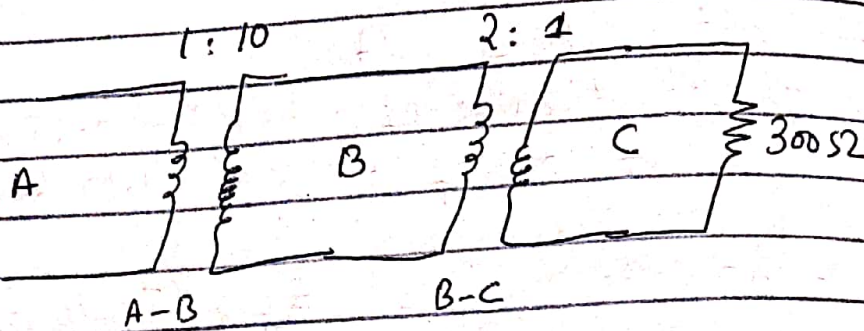
$$Z_{pu_{LT}} = \frac{Z_{HT} \left( \frac{KV_{LT}}{KV_{HT}} \right)^2 \times KVA_b}{KV_b^2 \times 1000}$$

$$Z_{pu(LT)} = \frac{Z_{HT} \times KVA_b}{(KV_{HT})^2 \times 1000} \quad - (1)$$

$$Z_{pu(HT)} = \frac{Z_{HT} \times (KVA_b)}{(KV_b)^2 \times 1000} \quad - (2)$$



Ex 3 parts of a single phase system are A, B, C are connected to each other through transformers as shown;



$X = 0.1 \text{ pu}$        $X = 0.08 \text{ pu}$   
 10000 kVA      10000 kVA  
 (13.8 - 138 kV)      (69 - 138) kV.

System base = Circuit B = 10000 kVA, 138 kV.

Draw impedance / reactance diagram neglecting the magnetizing current, resistance of transformer and X<sub>series</sub> line -

Determine the voltage regulation if voltage at load is 66 kV, assume voltage I/p to A B constant.

$$\underline{C} \quad (kVA)_b = 10000$$

$$(kV)_b = 138 \left(\frac{1}{2}\right) = 69 \text{ kV}$$

$$Z_{act} = 300 \Omega$$

$$Z_{base} = \frac{(kV_b)^2 \times 1000}{(kVA)_b} = \frac{(69)^2 \times 1000}{10000} = 476 \Omega$$

$$Z_{pu} = \frac{Z_{act}}{Z_{base}} = \frac{300}{476} = 0.63 \text{ pu}$$

B

$$Z_b = Z_c \left( \frac{2}{1} \right)^2 = 300 \left( \frac{4}{1} \right) = 1200 \Omega$$

$$Z_{base} = \frac{(138)^2 \times 1000}{10000} = 1900 \Omega$$

$$Z_{pu} = \frac{1200 \Omega}{1900 \Omega} = 0.63 \text{ pu.}$$

A

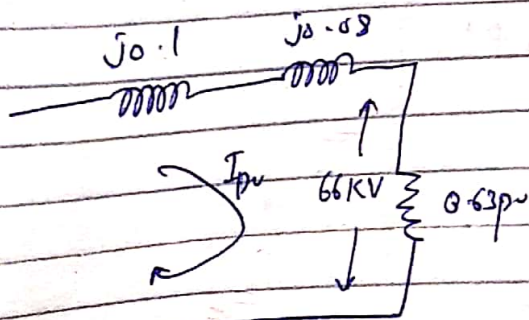
$$138 \left( \frac{1}{10} \right) = 13.8 \text{ kV}$$

$$Z = 300 \left( \frac{2}{1} \right)^2 \left( \frac{1}{10} \right)^2 = 12 \Omega$$

$$= 1200 \left( \frac{1}{10} \right)^2 = 12 \Omega$$

$$Z_{base} = \frac{(13.8)^2 \times 1000}{10000} = 19 \Omega$$

$$Z_{pu} = \frac{12}{19} = 0.63 \text{ pu}$$



$$V_L (\text{pu}) = \frac{66}{69} = 0.957 \text{ pu}$$

$$I_L = \frac{V_L}{Z_L} = \frac{0.957}{0.63} = 1.52 \text{ pu}$$

$$V_{NL} = 0.957 + I_L (j0.18)$$

$$V_{NL} = 0.995$$

Lecture

## Per Unit Impedances of three winding transformer.

In two winding T/F KVA rating of each winding is the same.

→ In three winding, it is different.

So to solve this problem, we need to convert all the quantities into single base @ single KVA rating.

These impedances are measured by short circuit tests.

$Z_{ps}$  = leakage imp measured in primary winding with secondary short circuited and tertiary is kept open.

$Z_{pt}$  = meas in pri, ter sh cr and tertiary kept open.

$Z_{st}$  = meas in sec, tert sh cr and primary kept open.

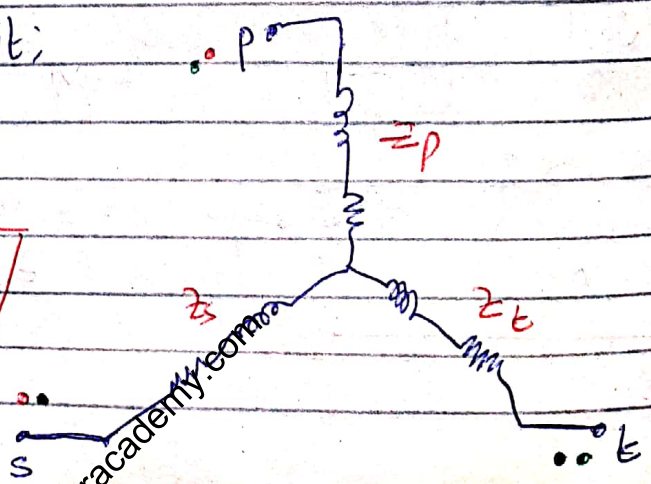
The equivalent circuit;

$Z_{ps}$   $Z_{pt}$   $Z_{st}$

$$Z_{ps} = Z_p + Z_s$$

$$Z_{pt} = Z_p + Z_t$$

$$Z_{st} = Z_s + Z_t$$



Solving simultaneously

$$\Rightarrow Z_p = \frac{1}{2} (Z_{ps} + Z_{pt} - Z_{st})$$

$$Z_s = \frac{1}{2} (Z_{st} + Z_{ps} - Z_{pt})$$

$$Z_t = \frac{1}{2} (Z_{pt} + Z_{st} - Z_{ps})$$

Three phase rating of a 3 winding transformer are;

P: Y connected 66 kV, 15 MVA

S: Y connected 13.2 kV, 10 MVA

T:  $\Delta$  connected 2.3 kV, 5 MVA.

$Z_{ps} = 7\%$  based on 15 MVA, 66 kV

$Z_{pt} = 9\%$  15 MVA, 66 kV

$Z_{st} = 8\%$  10 MVA, 13.2 kV

66 kV

Find  $Z_p$ ,  $Z_s$  and  $Z_t$  for the base of 15 MVA,

P: 15 MVA, 66 kV

S: 15 MVA,  $66 \times \frac{13.2}{66} = 13.2$  kV

T: 15 MVA,  $66 \times \frac{2.3}{66} = 2.3$  kV

No need to convert  $Z_{ps}$  and  $Z_{pt}$  b/c they are measured already in the same base (primary)

$$Z_{st} = (0.08) \left( \frac{15 \text{ MVA}}{10 \text{ MVA}} \right) \left( \frac{13.2}{13.2} \right)^2 = 12.1$$

$$\text{Now, } Z_p = \frac{1}{2} (j0.07 + j0.09 - j0.12) = j0.03 \text{ pu}$$

$$Z_s = \frac{1}{2} (j0.07 + j0.12 + j0.09) = j0.05 \text{ pu}$$

$$Z_t = \frac{1}{2} (j0.09 + j0.12 - j0.07) = j0.07 \text{ pu}$$

Convert all the quantities to a base of 10000 KVA, 6.6 KV.

$M_1$ : SM, 5000hp, pf = 0.8,  
rated V = 6.9 KV  
subtransient reactance,  $X'' = 0.17 \text{ pu}$

$M_2$  = SM, 3000hp, 1, 6.9KV, 0.15pu

$M_3$  = IM, 3600hp, , 6.9KV, 0.2 pu

↳ IM does not have a pf b/c it operates on a lagging pf (so depends on the load).

$$\text{KVA}_1 = 1.1 \times \text{hp} = 1.1 \times 5000 = 5500 \text{ KVA}$$

$$\text{KVA}_2 = 0.85 \times \text{hp} = 0.85 \times 3000 = 2550 \text{ KVA}$$

$$\text{KVA}_3 = 3500 \text{ KVA}$$

$$\text{pu of } M_1(\text{ms}) = 0.17 \left( \frac{10000}{5500} \right) \left( \frac{6.9}{6.6} \right)^2 =$$

$\frac{\text{new}}{\text{old}}$

$$pu \text{ of } M_2 (ns) = 0.5 \left( \frac{10000}{2550} \right) \left( \frac{6.9}{6.6} \right)^2 =$$

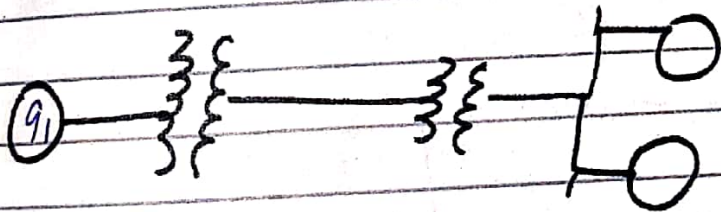
$$pu \text{ of } M_3 (ns) = 0.2 \left( \frac{10000}{3500} \right) \left( \frac{6.9}{6.6} \right)^2 =$$

A 30000 KVA, 13.8 KV 3  $\phi$  generator has  $X'' = 15\%$ .

The gen supplies two motors over a transmission line having T/Fs at both ends (fig)

Motors has rated i/p of 20000 and 10000 KVA. Both are 12.5 KV, and  $X'' = 0.2$

3 $\phi$  T/Fs at both ends are rated 3500 KVA, 13.2  $\Delta$  - 115 Y with leakage reactance 10%.



TL has reactance of  $80 \Omega$ .

Select the generator ie 30000 KVA, 13.8 KV as a base and transform all reactances to this.

$$(KV)_{b, TL} = 13.8 \times \frac{115}{13.2} = 120 \text{ KV (TL base)}$$

$$(KV)_{b (m)} = 13.8 \times \frac{15}{13.2} \times \frac{13.2}{115} = 13.8$$

$$V_{(m)} = 120 \left( \frac{13.2}{115} \right) = 13.8 \text{ kV}$$

$$X_{(TF_1)_{ns}} = (0.1) \left( \frac{30000}{35000} \right) \left( \frac{13.2}{13.8} \right)^2 = 0.078 \text{ pu}$$

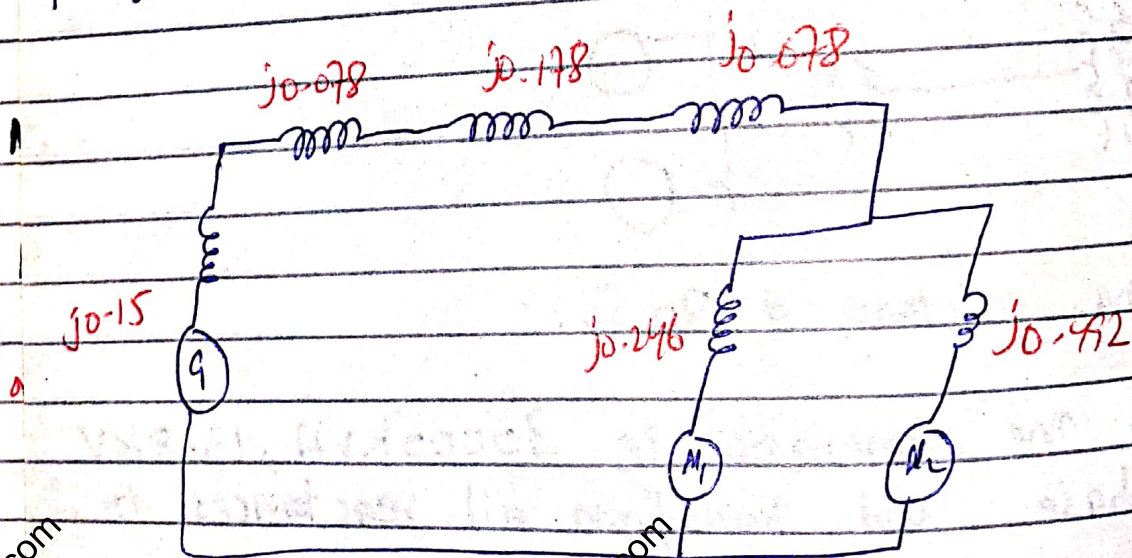
or  $\left( \frac{115}{120} \right)^2$

$$X_{(TF_2)_{ns}} = (0.1) \left( \frac{30000}{35000} \right) \left( \frac{12.5}{13.8} \right)^2 = 0.078 \text{ pu}$$

$$\text{pu of TL}_{(ns)} = \frac{80 \times 10^6}{(120)^2 \times 1000} = 0.167 \text{ pu}$$

$$\text{pu of } M_1_{(ns)} = 0.2 \left( \frac{30000}{20000} \right) \left( \frac{12.5}{13.8} \right)^2 = 0.246 \text{ pu}$$

$$\text{pu of } M_2_{(ns)} = 0.2 \left( \frac{30000}{10000} \right) \left( \frac{12.5}{13.8} \right)^2 = 0.492 \text{ pu}$$



300MVA, 20KV generator with  $X'' = 0.2 pu$   
 supplies number of motors over a 64 km long  
 transmission line. All motors = 13.2 KV

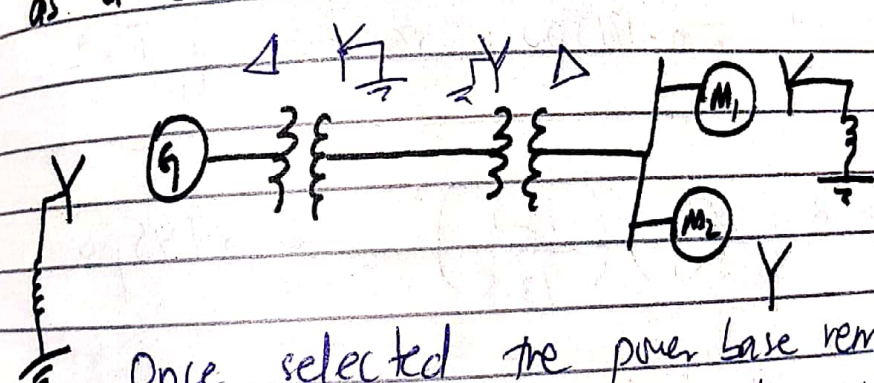
Neutral of  $M_1$  and grounded and  $M_2$  not grounded.  
 Rated  $I_{ps} = 200 MVA$  and  $100 MVA$ .  
 $X'' = 0.2 pu$  for both.

3 $\phi$  TFS  $T_1$ : 350MVA, 230/20 KV  
 with leakage reactance,  $X = 10\%$ .

$T_2$ : three  $\phi$  bank each rated 127/13.2KV  
 and 100MVA with  $X = 0.1 pu$

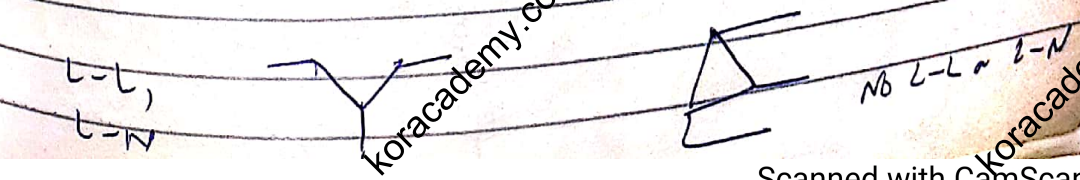
The series reactance of  $T \times L$ ,  $X = 0.5 \Omega/km$ .

Draw reactance diagram using generator rating  
 as a base.



Once selected the power base remains the same,  
 the only thing that changes is the voltage base.

$T_2$  = making 3 $\phi$  data from 1 $\phi$   
 $3 \times 100 = 300 MVA$   
 Line to line voltage ratio =  $\frac{\sqrt{3} (127)}{13.2}$





$$T_{KL} = 20 \text{ kV} \left( \frac{230 \text{ kV}}{20 \text{ kV}} \right) = 230 \text{ kV}$$

$$M = 230 \left( \frac{13.2}{127 \times \sqrt{3}} \right) = 13.8 \text{ kV}$$

$$X_{(TF)}_{NS} = 0.1 \times \frac{300}{350} = 0.857 \text{ pu}$$

voltage base if you consider primary side, new base and old base so in ac 20. if you consider transmission secondary side, old and new base both ac 230.

$$X_{(TF)}_{NS} = 0.1 \times \frac{300}{230} \times \left( \frac{13.2}{13.8} \right)^2 = 0.0915 \text{ pu}$$

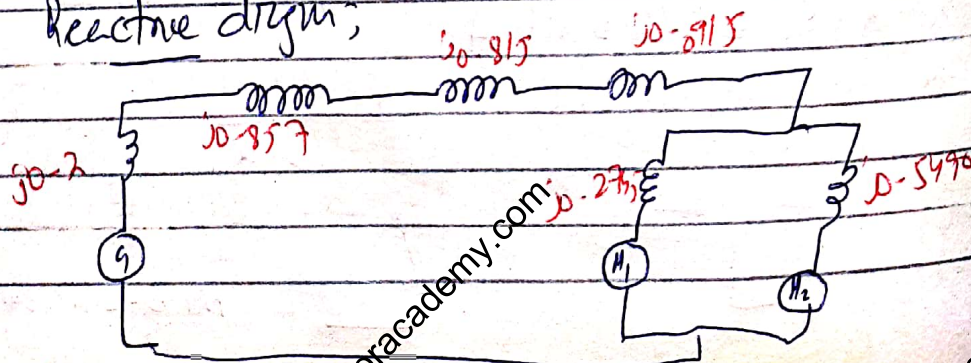
$$\text{Transmission line, } X_{\text{act}} = \frac{V^2}{P} = \frac{230^2}{300} = 176.3 \text{ pu}$$

$$\frac{0.5 \times 64}{176.3} = 0.1815 \text{ pu} = \text{reactance of T x L.}$$

$$X_{M1(\text{ns})} = 0.2 \left( \frac{300}{200} \right) \left( \frac{13.2}{13.8} \right)^2 = 0.2745 \text{ pu}$$

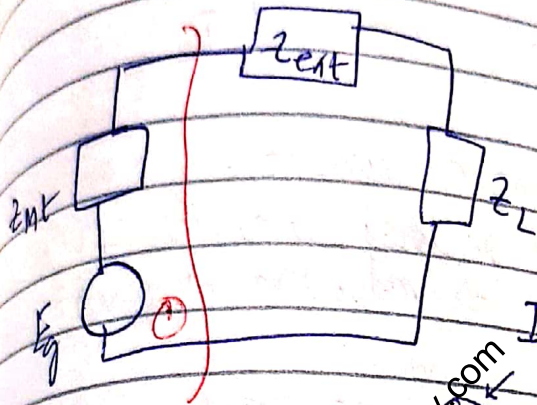
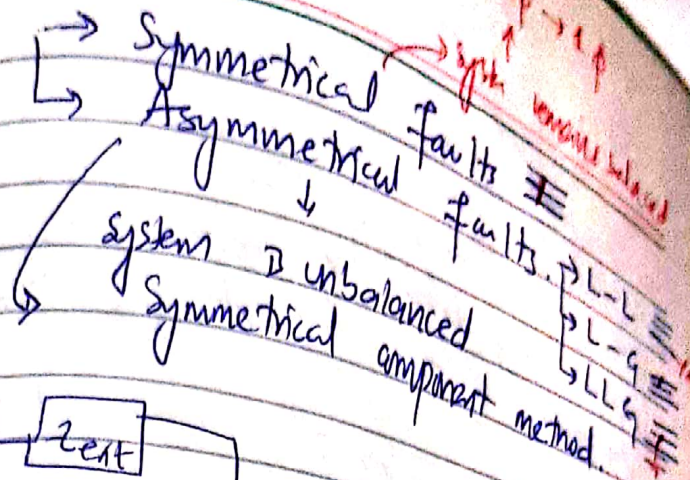
$$X_{M2(\text{ns})} = 0.2 \left( \frac{300}{100} \right) \left( \frac{13.2}{13.8} \right)^2 = 0.5490 \text{ pu}$$

Reactive diagram;



# Lecture

## Faults



As  $I = V/Z$

Normal current;

$$I_n = \frac{E_g}{Z_{int} + Z_{ext} + Z_L}$$

If fault at generator end:

$$I_{f1} = \frac{E_g}{Z_{int}} \rightarrow \text{(ii)}$$

If fault at load end;

$$I_{f2} = \frac{E_g}{Z_{int} + Z_{ext}} \rightarrow \text{(iii)}$$

### Duties of Circuit breaker;

- i. To carry normal current for an infinite period of time.
- ii. To carry very high current for a very short period of time.
- iii. To interrupt high current if it sustains.

When a fault occurs in a power system, the current is determined by three things -

- Internal voltage of the source.
- Internal impedance of generator.
- Impedance of the network (G → fault)

Fault cur  $I_n$ , few cycles  $I_s$ , sustained  $I_c$ .

→ These 3 differ b/c of armature current.

which opposes the main flux → reduction in current.   
 → produces armature flux

Initial - steady state ⇒ change in current.

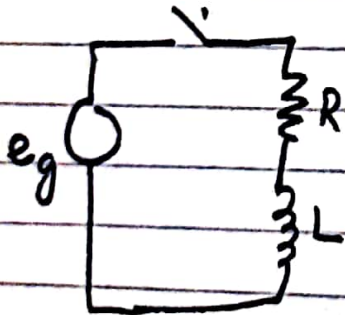
$X, X', X''$  changes b/c  $E_g$  is the same.

$$\frac{E_g}{I}, \frac{E_g}{I'}, \frac{E_g}{I''}$$

Consider:

$$e_g = V_m \sin(\omega t + \alpha)$$

$t=0$  at the time of applied voltage.



$\alpha$  determines the magnitude of voltage when the circuit is just closed.

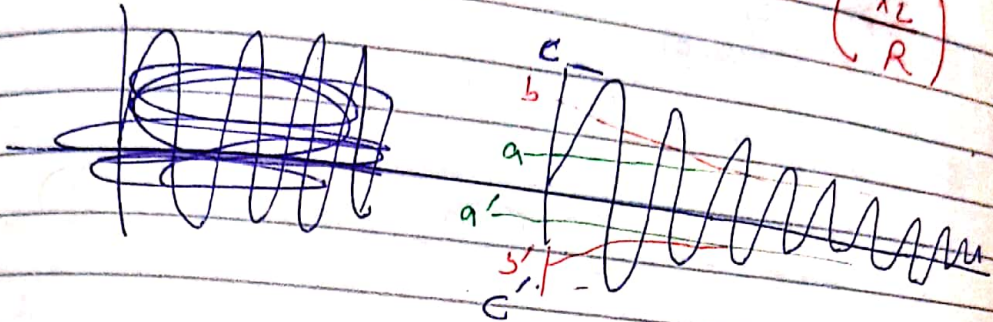
$$V_m \sin(\omega t + \alpha) = iR + L \frac{di}{dt}$$

$i = i_{ac} + i_{dc}$  same time.  
 due to voltage source.  $n \rightarrow$  due to transient and decay after

$$i = \frac{V_m}{Z} \left[ \sin(\omega t + \alpha - \theta) - e^{-Rt/L} \sin(\alpha - \theta) \right]$$

$$Z = \sqrt{R^2 + (WL)^2}$$

$$\theta = \tan^{-1} \left( \frac{X_L}{R} \right)$$



oa → steady state current,  $I = oa \times 0.707 \rightarrow$  rms value.

$X = E_g / I =$  Direct axis steady state reactance / synchronous reactance.

generators are *quite* large compared to their internal resistance.

ob → maximum transient current,  $I' = 0.707 (ob) \rightarrow$  rms.

$X' = E_g / I' \rightarrow$  direct axis transient reactance.

oc → subtransient reactance,  $I'' = 0.707 (oc) \rightarrow$  rms.

just at the occurrence of fault.

$X'' = E_g / I'' \rightarrow$  direct axis subtransient reactance.

$$X'' < X' < X$$

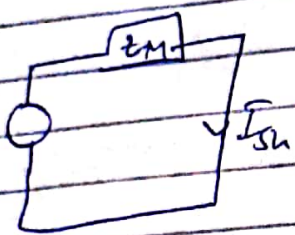
→ Interrupting capacity of circuit breakers;  
 $X'' \rightarrow \text{G}$        $X' \rightarrow \text{SM}$        $\text{IM } X$

$$\text{Fault MVA} = \sqrt{3} \times \text{Nominal KV} \times I_{sc} \times 10^{-3}$$

$$Z_{pu} = \frac{I_{base}}{I_{short}}$$

As S.C MVA =  $\sqrt{3} \times N \text{ KV} \times I_{sc} \times 10^{-3}$

$$I_{sc} = \frac{\text{SC MVA}}{\sqrt{3} \times N \text{ KV} \times 10^{-3}} \quad \text{--- (1)}$$



$$I_{sc} = \frac{N \text{ KV} / \sqrt{3} \times 10^{+3}}{Z_M} \quad \text{--- (2)}$$

$$Z_M = \frac{N \text{ KV} / \sqrt{3} \times 10^{+3}}{I_{sc}} \quad \text{--- (3)}$$

(1)  $\Rightarrow$  (2)

$$Z_M = \frac{N \text{ KV} / \sqrt{3} \times 10^{+3} \times \sqrt{3} \times N \text{ KV} \times 10^{-3}}{\text{SC MVA}}$$

$$Z_M = \frac{(N \text{ KV})^2}{\text{SC MVA}}$$

As  $Z_{pu} = \frac{Z_{act} \times \text{MVA}}{(KV_b)^2}$

$$\Rightarrow Z_{pu} = \frac{(N \text{ KV})^2}{\text{SC MVA}} \times \frac{(\text{MVA})_b}{(1 \text{ KV})^2}$$

Assume  $(KV)_b = N \text{ KV}$

$$\Rightarrow Z_{pu} = \frac{(\text{MVA})_b}{\text{SC MVA}}$$

$$Z_{pu} = \frac{\sqrt{3} \times (\text{KV})_b \times I_{base} \times 10^{-3}}{\sqrt{3} \times (\text{MKV}) \times I_{sc} \times 10^{-3}}$$

$$\rightarrow Z_{pu} = \frac{I_{base}}{I_{sc}}$$

## Lecture

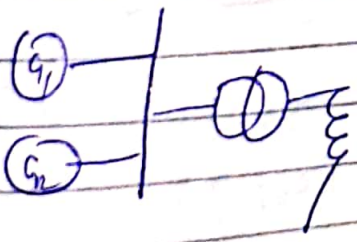
Two generators are connected in parallel. ~~load is on the LT side of a 3 $\phi$   $\Delta$ -Y.~~

Gen 1 = 50000 KVA, 13.8 KV }  $X'' = 0.25$   
 Gen 2 = 25000 KVA, 13.8 KV }  
 T/F = 75000 KVA, 13.8  $\Delta$ -69Y,  $X = 10$

Before fault HT side  $V = 66$  KV, T/F is unloaded and no circulating current s/w gens.

*Circulating current flows s/w the generators when both have different voltage ratings.*

$I_g''$ ,  $I_f = ?$  when a 3 $\phi$  s.c occurs on HT side.

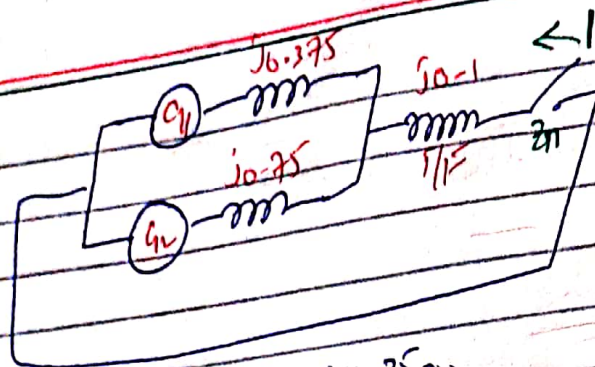


Let the selected base is 75000 KVA, 69 KV. (T/F)

$$KV_b (LT) = 69 \left( \frac{13.8}{69} \right) = 13.8 \text{ KV}$$

$$X_{g1} (ns) = 0.25 \left( \frac{75000}{50000} \right) \left( \frac{13.8}{13.8} \right)^2 = j0.375 \text{ pu}$$

$$X_{g2} (ns) = 0.25 \left( \frac{75000}{25000} \right) \left( \frac{13.8}{13.8} \right)^2 = j0.75 \text{ pu}$$



$$V_f = \frac{66}{69} = 0.957 \text{ pu}$$

$$Z_n = \frac{(j0.375)(j0.75)}{j0.375 + j0.75} + j0.1$$

$$Z_n = j0.35 \text{ pu}$$

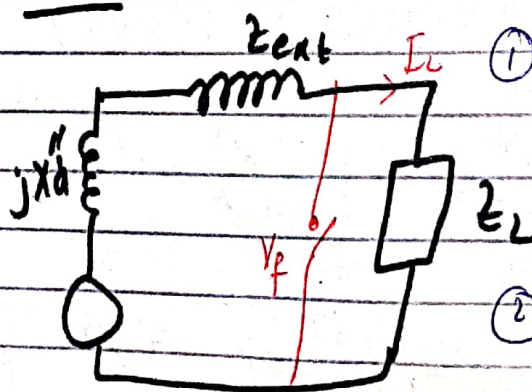
$$I_f'' = \frac{V_f}{Z_f} = \frac{0.95}{j0.35} = -j2.714 \text{ pu}$$

$$I_{g1}'' = \frac{I_f'' (j0.75)}{j0.75 + j0.375} = -j1.823 \text{ pu}$$

$$I_{g2}'' = \frac{I_f'' (0.375)}{j0.75 + j0.375} = -j0.911 \text{ pu}$$

For actual ~~for~~ current multiply with base i.e.  $\frac{75000}{\sqrt{3} \times 69}$

### Internal voltages of Loaded machines under transient conditions.



$$\textcircled{1} \quad Z_m = \frac{Z_{ext} + jX_d'' \times Z_L}{Z_{ext} + jX_d'' + Z_L}$$

$$\textcircled{2} \quad I_f'' = \frac{V_f}{Z_m} = \frac{V_f (Z_{ext} + jX_d'')}{Z_{ext} + jX_d'' + Z_L}$$

$$I_f'' = \frac{E''}{jX_d'' + Z_{ext}} \quad \textcircled{3}$$

$$\text{Qad ③} \Rightarrow \frac{E''}{jX_d'' + z_{ext}} = \frac{V_t (z_{ext} + jX_d'' + z_L)}{z_L (z_{ext} + jX_d'')}$$

$$E'' = I_L (z_{ext} + jX_d'' + z_L)$$

$$\Rightarrow E'' = I_L (z_{ext} + z_L) + I_L (jX_d'')$$

$$E'' = V_t + I_L X_d''$$

$$E' = V_t + I_L X_d'$$

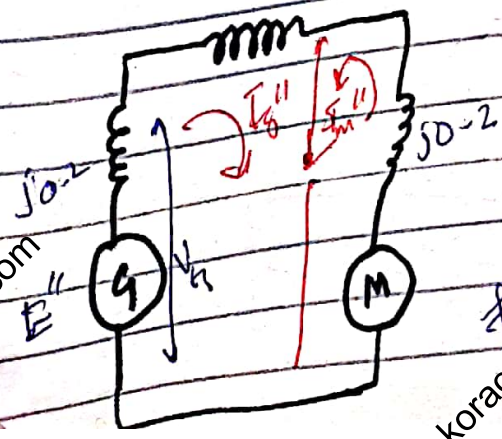
$$E''_{\text{motor}} = V_t - I_L X_d'' \Rightarrow E'_m = V_t - I_L X_d'$$

For unloaded generators,  $E' = E'' = E = E_g$   
 In loaded conditions,  $E' \neq E'' \neq E$

An alternator and SM are rated 30000 kVA, 13.2 kV with  $X'' = X'_m = 0.2 \text{ pu}$ .  
 The line connecting them,  $X_L = 0.1 \text{ pu}$ .  
 Motor  $\text{p.f.} = 20000 \text{ kVA}, 0.8 \text{ pf}, 12.8 \text{ kV}$

A symmetrical 3 $\phi$  fault occurs at the motor end.

Consider system base as base;  
 30000 kVA, 13.2 kV



$$V_f (\text{pu}) = \frac{12.8}{13.2} = 0.97 \text{ pu}$$



$$I_b = \frac{30000}{\sqrt{3} \times 13.2} = 1312 \text{ A.}$$

$$I_L = \frac{20000}{\sqrt{3} \times 12.8 \times 0.8} = 1128 \angle 36.8^\circ$$

$$\frac{I}{I_{pu}} = \frac{I_{act}}{I_b} = \frac{1128 \angle 36.8^\circ}{1312} = 0.86 \angle 36.8^\circ \text{ pu.}$$

$$E_g'' = V_t + j I_L X_d''$$

$$\text{As } V_t = V_f + I_a Z_{ext} = (0.918 + j0.069) \text{ pu}$$

$$E_g'' = 0.814 + j0.07 \text{ pu}$$

$$E_m'' = V_{t_m} - j I_L X_L'' = (0.97 - j0.86 \angle 36.8^\circ)(j0.2)$$

$$\Rightarrow E_m'' = (1.074 - j0.138) \text{ pu}$$

$$I_g'' = \frac{E_g''}{j0.3} \rightarrow \text{generate to fault point}$$

$$I_m'' = \frac{E_m''}{j0.2} \rightarrow \text{motor to fault point.}$$

$$I_f'' = I_g'' + I_m'' = -j8.08 \text{ pu}$$

Fault MVA = ?

$$I_f''_{\text{actual}} = (-j8.08) \times 1312 = \boxed{-j10600 \text{ A}}$$

$$\begin{aligned} \text{Fault MVA} &= \sqrt{3} \times V_L \times I_{sc} \times 10^{-3} \\ &= 242.4 \text{ MVA.} \end{aligned}$$